Math 131 - April 29, 2016

Final's Week Resources

- Blake's office hours (TBA)
- Marie Jose's office hours (TBA)
- Calculus help room
- RPMs

Test Review Problems

1. True/False

    (a) The function $f(x) = e^x$ is the inverse of $g(x) = \ln x$

    (b) $\lim_{x \to 0}(\sin x)/x = 0$

    (c) $f(x) = |x|$ is continuous for all x.

    (d) A function can have two different horizontal asymptotes.

    (e) If $-x^2 \le f(x) \le x^4$ for all x in $[-1, 1]$ then $\lim_{x \to 0} f(x) = 0$

    (f) If $f''(c) = 0$ then $x = c$ is an inflection point.

    (g) If $f(x)$ is continuous then it is differentiable.

    (h) If $f(x)$ is differentiable then it is continuous.

    (i) f and g are continuous on $[a, b]$ and $f(x) \ge g(x) \ge 0$, $m \le f(x) \le M$. Which are true:

    - $\int_a^b f(x)\, dx \ge 0$
    - $\int_a^b f(x)\, dx \ge \int_a^b g(x)\, dx$
    - $m(b - a) \le \int_a^b f(x)\, dx \le M(b - a)$

2. Find the maximum and minimum of $f(x) = x^3 - 6x^2 + 9x + 1$ on $[2, 4]$.

3. Find $\frac{d}{dx} \sin^2(x^2)$

4. What is the slope of the line tangent to $x^2 + 3x^2 y^2 + 5y^3 + y = 8$ at the point $(2, 0)$?

5. Find the equation of the line tangent to the curve $y = x^2 + e^x$ at the point $(1, 1 + e)$.

6. A particle's position at time t is $s(t) = \sin 2t$. What is the acceleration at time t?

7. Find the average rate of change of $f(x) = x + 6/x$ on the interval $[1, 3]$.

8. Find where $f(x) = 12/(x^2 + 6x + 12)$ is increasing.

9. Find $\lim_{x \to 0}(e^x - 1 - x)/(\cos x - 1)$

10. Find the minimum of $f(x) = (x^4 + 1/x)e^{-x}$ on the interval $(0, \infty)$.

11. Use a linear approximation of $f(x) = x^{4/3}$ at $a = 1000$ to approximate $(1006)^{4/3}$.

12. The altitude of a triangle is increasing at a rate of 1 cm/min while the area of the triangle is increasing at a rate of 2 cm^2/min. At what rate is the bae of the triangle changing when the altitude is 10 cm and the area is 100 cm^2.

13. Find the anti-derivative of $f(x) = x^3 + \sin x$

14. Find the minimum of $f(x) = x^2 \ln x$ on $[0, 2]$.

15. Let $f(x) = (\ln(1 + 2x))/\cos 3x$. Find $f'(0)$

16. A particle moves on a vertical line so that its y-coordinate at time t is $y = t^3 - 12t + 3$, for $t \geq 0$. When is the particle moving up?

17. Find the equation of the tangent line to the curve $x^3 + y^3 = 6xy$ at the point $(3, 3)$.

18. Find the equation of the tangent line to the curve $y = \sqrt{\sin^2 x + x^2}$ at (π, π)

19. Let $f(x) = e^x/\sin x$. Find where $f'(x) = 0$.

20. Find $\lim_{x \to \infty} \sqrt{3x^2 + 1}/(2x - 4)$

21. Suppose $f'(x) = e^x \sin x$. On the interval $(0, 2\pi)$, where is $f(x)$ concave down?

22. Find $\lim_{x \to 1} x^{1/(1-x)}$

23. What are all the indeterminate forms?

24. Find the inflection points of $f(x) = e^{-2x^2}$.

25. $f(x) = x^{1/x}$. Find $f'(2)$.

26. Find all asymptotes of $f(x) = \frac{x^2 - 5x + 6}{3x^2 + 4x + 1}$

27. A spotlight on the ground shines on a wall 12 meters away. If a man 2 meters tall walks away from the spotlight towards the building at the rate of 1.6 m/s, how fast is the length of his shawdow decreasing when he is 4 m from the building.

28. Find $\lim_{x \to \infty} \ln((x + 1)/(3x))$

29. Find the inverse of $f(x) = (x + 1)/(2x + 1)$

30. Use Riemann sums to compute $\int_0^4 (x+1)\, dx$. Check your solution with the fundamental theorem of calculus.

31. If $\int_0^7 g(x)\, dx = 20$, $\int_4^7 g(x)\, dx = 4$, and $\int_0^1 g(x)\, dx = 7$ then what is $\int_1^4 g(x)\, dx$.

32. Find $\int_0^{\pi/4} \sec^2 x + \cos x\, dx$

33. Approximate $\int_{-4}^4 x^2 - 2x\, dx$ using a right hand sum with $n = 4$.

34. Given theat $f(x) = \int_1^x \frac{1}{t}\, dt$, find $f'(2)$

35. Let $F(x)$ be the antiderivative of $f(x) = 5x^4 - 2x^5$. Suppose $F(0) = 4$. Find $F(1)$.

36. Find $\sum_{k=0}^5 k$

37. Find $\int_1^2 (6x^2 - 4x + 5)\, dx$

38. Write the integral as a limit of Riemann sums: $\int_0^4 (2x^2 + 3)\, dx$

39. Write the integral as a limit of Riemann sums: $\int_1^5 (2x^2 + 3)\, dx$

40. Write the limit as a definite integral: $\lim_{n \to \infty} \sum_{i=1}^n \left(-1 + \frac{3i}{n}\right)^2 \left(\frac{3}{n}\right)$

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