

# Möbius Strips and More

① Möbius strip -- only one side!

② Cut it in half, get ... something.

③ Take a long, thin strip, give it two twists and tape it.

④ Is this the same as the Möbius strip/2? [Reconfigure the M.S./2 to look like a figure-eight also.]  
(discuss)

⑤ put each in "box form," see the difference

⑥ How to prove it?

One way to show that two things are different is to do the same thing to each one and see if you get the same result. [An invariant]

⑦ Cut each in half -- two interlocked loops.

Crumple each one: They are interlocked differently!

⑧ The M.S. only has one side; its surface is connected.  
[Distinguish a shape vs its surface]

What is the shape of its surface?

⑨ Take two strips on top of each other, and make a "doubled-over" Möbius strip. Then, tape it. Now, the paper is in the shape of the surface.

⑩ Fold it into box form... same thing!  
So, this "flat form" or "box form" is useful...

⑪ To get something<sup>else</sup> with one side, we need 3 twists (two won't work).  
What is the shape of that "side?"  
For one thing, it's knotted!

Connecting a couple of these ideas with math you've already seen... (next)

After ⑩:

$$(x-3)^2 + Ax + B$$

$$x^2 - 6x + 9 + Ax + B$$

$$x^2 + [A-6]x + [B+9]$$

$$x^2 + 3x + 2$$

$$(x+2)(x+1)$$

Are

$$(x-3)^2 + 9x - 7 \quad \text{and}$$

$$(x+2)(x+2) - x - 2$$

the same?

(Have them do it)

How did you solve it? With a "standard form."

There is another "standard form" for a polynomial, which is good for giving you graphical information.

- What is it?
- $a(x-h)^2 + c$